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DRAG REDUCTION BY CATION SURFACTANTS: THE RELATION TO
PHYSICOCHEMICAL AND MICELLAR CHARACTERISTICS
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UDC $532.517 .4: 661.185 .23$
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It is shown that systems containing the cationic surfactant $\alpha$-naphthol begin to reduce the hydrodynamic resistance at concentrations of $0.02-0.05 \%$, at which solutions contain nonspherical micelles of a particular size.

We have previously shown [1] that the combination of cetylpyridinium chloride (CPC1) with $\alpha$-naphthol with a 1:1 ratio of the components reduces the drag in the turbulent flow of a liquid (water). Here we consider the drag reduction for water caused by various cationic surfactants in the presence of $\alpha$-naphthol, and we derive a relationship between the reduction in the drag and the physicochemical parameters of the solutions.

We chose the cationic surfactants cetyl- $\gamma-\mathrm{picolinium}$ bromide ( $C-\gamma-\mathrm{PicBr}$ ), cetylpyridinium bromide ( CPBr ), cetylpyridinium iodide (CPI), the hydrochlorides and hydroiodides of alkyl-


in which the lengths of the alkyl chains $R$ were 12 and 16 carbon atoms.
The drag was measured with a glass tube of length 4 m and diameter 5.45 mm for a Reynolds number of 10,000 . The drag reduction $(\Delta \lambda / \lambda)$ was calculated from

$$
\frac{\Delta \lambda}{\lambda^{-}}=1-\frac{\tau_{2}^{2}}{\tau_{1}^{2}} \frac{\Delta P_{2}}{\Delta P_{1}}
$$

The viscosities of the solutions were determined with a BPZh-2 capillary viscometer, while the density was determined by a pycnometer method. The IR spectra of these surfactants dissolved in carbon tetrachloride with and without $\alpha$-naphthol were recorded with a UR-20 spectrophotometer in the $O H$ stretching region. The optical density of Sudan II (a water insoluble dye solubilized by the surfactants) was measured with an $\mathrm{SF}-16$ spectrophotometer at 550 nm .

The measurements (Fig. 1) show that systems such as $\mathrm{C}-\gamma-\mathrm{PicBr}-\alpha-\mathrm{naphthol}, \mathrm{CPBr}-\alpha-$ naphthol, and CPI- $\alpha$-naphthol reduce the drag at the very low overall concentration of

[^0]

Fig. 1


Fig. 2

Fig. 1. Drag reduction ( $\Delta \lambda / \lambda, \%$ ) for cationic surfactants with $\alpha$-naphthol at various concentrations (C, \%) in relation to temperature $\left(t,{ }^{\circ} \mathrm{C}\right)$. CPI- $\alpha$-naphthol: 1) $\mathrm{C}_{1}=0.075$, $\mathrm{C}_{2}=0.016$; 2) $\left.\mathrm{C}_{1}=0.037, \mathrm{C}_{2}=0.008 ; 3\right) \mathrm{C}_{1}=0.018 ; \mathrm{C}_{2}=$ $0.004 ; \mathrm{CPBr}-\alpha$-naphtho1; 4) $\mathrm{C}_{3}=0.060, \mathrm{C}_{2}=0.022$; 5) $\mathrm{C}_{3}=$ $0.030, C_{2}=0.011 ; ~ C-\gamma-\mathrm{PicBr}-\alpha$-naphthol: 6) $\mathrm{C}_{4}=0.100$, $\mathrm{C}_{2}=0.048$; 7) $\mathrm{C}_{4}=0.050, \mathrm{C}_{2}=0.024$.
Fig. 2. Effects of $\alpha$-naphthol concentration on the physicochemical parameters of CPC1- $\alpha$-naphthol at $\mathrm{C}_{5}=0.007 \mathrm{M}$ and $\mathrm{t}=25^{\circ} \mathrm{C}$ : 1) relative viscosity $\mathrm{n}_{\mathrm{re}}$; 2) drag reduction ( $\Delta \lambda / \lambda, \%$ ) ; 3) ratio of semiaxes ( $\alpha / \mathrm{b}$ ); 4) optical density A of solutions in this system containing Sudan II.
$0.02-0.05 \%$. This is well below the levels of all surfactants reported in the literature as reducing hydrodynamic resistance in liquids [2-4]. The structures of the surfactant solutions were examined by reference to the physicochemical parameters (Fig. 2). The viscosities of surfactant solutions containing $\alpha$-naphthol were plotted as a function of the $\alpha-$ naphthol concentration; there is a kink showing a sharp increase in viscosity at a particular $\alpha$-naphthol level. This indicates [1] that the micellar structures at that point go over from spherical to aspheric. The concentration is called the second critical micelle concentration ( $\mathrm{CMCII}_{I}$ ) ; the first critical micelle concentration (CMCI) is the surfactant concentration at which spherical micelles are formed.

This aspheric transition gives rods, which involves compression and compaction of the micelles [5]. This reduces the solubilizing action of the micelles by comparison with the spherical case. There is a marked reduction in the solubilizing capacity for Sudan II in surfactants combined with $\alpha$-naphtho1 (Fig. 2) at a particular concentration of the latter, which also indicates that aspheric micelles are formed. The drag reduction occurs approximately at the concentration CMCII (Fig. 3), i.e., the published data for CMCII for various surfactants serve to characterize not only the physicochemical properties but also the drag performance. These values constitute the minimum surfactant concentration necessary to reduce the frictional loss in the turbulent flow of water.

The considerable increase in viscosity in surfactant-a-naphthol solutions at concentrations above CMCII indicates [1] that aspheric micelles occur. Coombe's equation [5] describes the relative viscosity of a surfactant solution as a function of the semiaxes of the micelles, which are considered as flattened ellipsoids of rotation, and Guth and Simha [6] transformed this to the form

$$
a / b=1+0.663 \exp (3.46 \varphi)
$$

where $\varphi$ is found from the observed relative viscosity;

$$
\eta=1+2.5 \varphi+14.1 \varphi^{2} .
$$

These equations have been widely used in the literature to estimate the shapes of micelles $[7,8]$. The ratio of the semiaxes at which the drag drop occurs is in the range from 2 to 14 for various surfactants. The minimum ratio at which the effect originates corresponds to a concentration of surfactant close to the concentration of $\mathrm{CMC}_{I I}$.


Fig. 3. Physicochemical parameters of aqueous solutions of CPI in relation to concentration ( $\mathrm{C}, \mathrm{M}$ ) at $\mathrm{t}=45^{\circ} \mathrm{C}$ : 1) relative viscosity Mrel; 2) drag reduction ( $\Delta \lambda / \lambda, \%$ ) 3) ratio of semiaxes, $a / b$.

Fig. 4. IR spectra: effects of CPCl on the absorption $A$ in the OH -stretching band of $\alpha$-naphthol: 1) $\alpha$-naphthol in $\mathrm{CCl}_{4}$; 2) $\mathrm{CPCl}+$ $\alpha$-naphtho1 in $\mathrm{CC1}_{4} ; \mathrm{C}_{2}=0.0067 \mathrm{M}, \mathrm{C}_{5}=0.0033 \mathrm{M}$.

A detailed discussion of the relationship of the effect to CMCII [1,9] indicates that the reduced drag begins at a surfactant concentration equal to or somewhat less than CMCII; in the system CPCI- - -naphthol the concentration is less than CMCII by a factor 1.1-1.2 (Fig. 2). Figure 3 shows that the reduction in drag occurs at a CPI concentration less than CMCII by a factor 1.6. Spherical micelles exist in solutions with concentrations less than CMCII under static conditions. On the other hand, the micelles are oriented in a flow and are deformed [10]. One consequence of this is that the micelles become aspheric at concentrations lower than those relating to static conditions, because the drag reduction sometimes sets in at surfactant concentrations somewhat less than CMCII.

One result of the orientation may also be that the rod micelles link up into filaments; these resemble the macromolecules of linear polymers as regards behavior in a flow. The surfactants reduce the drag by a mechanism analogous to that applicable to polymers. One of the disadvantages of polymers that reduce the drag is that the performance decreases with time on account of irreversible mechanical destruction of the macromolecules in the flow [11]. Polymer-type filamentary micelles are also undoubtedly damaged mechanically, but micelle formation is reversible [12], so the micelles will recover their properties when the factors causing destruction are eliminated. This itself has disadvantages, because we do not know how to synthesize a micellar structure that reduces the drag. Such structures exist only under particular conditions, which are governed by the temperature, the nature of the material, the concentration, and various other factors. We know of only a few systems that reduce the drag in water. It is therefore necessary to define new additives. The physicochemical parameter characterizing the hydrodynamic effect of a surfactant may be taken as $\mathrm{CMC}_{\text {II }}$.

The above surfactants ( $\mathrm{CPCl}, \mathrm{CPBr}, \mathrm{CPI}, \mathrm{C}-\gamma-\mathrm{PicBr}$ ) with $\alpha$-naphthol reduce the drag, but there are compounds that do not do this in the presence of $\alpha$-naphthol at any concentration or ratio of the components (Table 1). Examples are substances such as hydrogen halides of alkylimidazolines, alkylamidoamines, and alkylamines.

The viscosity in relation to $\alpha$-naphthol concentration shows that aspheric micelles are not formed in these solutions; these surfactants have NH groups in the hydrophilic parts of the molecule and low degrees of dissociation of the molecules in micelles [13].

IR spectroscopy in carbon tetrachloride (as a model for undissociated surfactant molecules) has shown that $\alpha$-naphthol interacts via hydrogen bonds with the hydrophilic part of the surfactant molecule (Fig. 4). The electron-density distributions in the cation and anion [14] indicate that $\alpha$-naphthol can interact only with the anion molecule not containing NH groups, and it does not interact with the surface-active cation. The $\alpha$-naphthol interacts with cationic surfactants via the NH groups in the hydrophilic part of the surfactant, i.e., $\alpha$-naphthol interacts with the undissociated molecules in the micelle in aqueous solution and accumulates in the hydrophilic part of the latter. When $\alpha$-naphthol is solubilized by a

TABLE 1. Effects of Structure of Cationic Surfactant on the Formation of Aspheric Micelles and Drag Reduction in Aqueous Solutions Containing $\alpha$-Naphthol

| Surfactant | Colloid-chemical properties and hydrodynamic resistance in solutions of surfactant with $\alpha$-naphthot |  |  |
| :---: | :---: | :---: | :---: |
|  | form of micelles: aspheric $(t)$, spherical (-); | drag: no reduction (-), reducm tion ( + ) | constants for ratio of $\mathrm{CMC}_{\text {II }}$ and $\alpha-$ naphthol concentration ( $\mathrm{K}=\mathrm{CMC}_{I I} / \mathrm{C}_{2}$ ) for various cationic surfactants with $\alpha$-naphthol at $\mathrm{t}=45^{\circ}$ |
| Setylisoquinolinium bromide | + | + | 4,44 |
| Cetylpyridinium choridee | + | $+$ | 2,50 |
| Cetylpyridinium bromide | $+$ | $+$ | 1,51 |
| Cetyl- $\gamma$-picolinium bromide | $+$ | + | 1,05 |
| Cetylimidazolinium chtoride | - | - | - |
| Cetylamidoammonium chiloride | - | - | - |
| Cetylammonium chloride | - | - | - |

surfactant having a high degree of dissociation of the molecules in the micelle, most of the compound will appear in the hydrophobic part. Literature data [13] confirm the nonuniform distribution of $\alpha$-naphthol in the hydrophilic and hydrophobic parts of micelles, where the structure of the surfactant is the relevant feature. The presence of $\alpha$-naphthol in the hydrophilic part of the micelles interferes with the transition to aspheric form, since this must be accompanied by a reduction in the distance between the hydrophilic parts [15]. Therefore, a surfactant that contains NH groups in the hydrophilic part or has a low degree of dissociation cannot reduce the hydrodynamic resistance of water. This provides a way of selecting surfactants that can reduce the drag in the presence of $\alpha$-naphthol. This occurs in any surfactant whose hydrophilic part does not contain functional groups that are proton donors ( $-\mathrm{NH}-,-\mathrm{OH}$, , etc.) and which have a high degree of molecular dissociation in the micelles [13].

It has been shown [13] that the degree of dissociation of a cationic surfactant is directly proportional to the dipole moment; we can therefore list surfactants that will reduce the drag in the presence of $\alpha$-naphthol. Examples are alkylisoquinolinium and alkyllutidinium halides. The latter are synthesized from coal-tar products and at present have no particular application.

## NOTATION

$\Delta \lambda / \lambda$, drag reduction, $\%$; t, temperature, ${ }^{\circ} \mathrm{C} ; \mathrm{C}$, concentration, \%, mole/liter; $\mathrm{C}_{1}$, concentration of CPI solution, \%, mole/liter; $\mathrm{C}_{3}$, concentrationof CPBr solution, \%; $\mathrm{C}_{4}$, concentration of $\mathrm{C}-\gamma-\mathrm{PicBr}$ solution, $\%$; $\mathrm{C}_{5}$, concentration of CPCl solution, mole/liter; $\eta$, relative viscosity; $a / b$, micelle semiaxis ratio; $\tau_{1}$, water efflux time, sec; $\tau_{2}$, solution efflux times, sec; $P_{1}$, water pressure difference, mpater column; $P_{2}$, pressure difference in flowing solutions; A, absorption; $v$, frequency, $\mathrm{cm}^{-1}$; HR , drag; $\mathrm{C}_{2}$, concentration of $\alpha$-naphthol, \%, mole/ liter; $\varphi$, volume fraction of micelles.

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EXPERIMENTAL STUDY OF TRANSVERSE MASS EXCHANGE IN THE
FLOW OF POLYOXYETHYLENE SOLUTIONS IN A ROUND PIPE
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A method is proposed for investigating the transverse mass exchange in the turbulent flow of polyoxyethylene solutions in a pipe using the phenomenon of nuclear magnetic resonance.

Investigations of the influence of polymer admixtures on the reduction of hydrodynamic resistance in the turbulent flow of polyoxyethylene solutions in pipes by traditional methods are described in [1].

However, these methods introduce a disturbance into the investigated medium, which can lead to considerable errors when measuring in pipes of small diameter. As for methods based on recording particle tracks [2], they also are not free of important drawbacks, especially when investigating flows of polymer solutions, since polymers, while effectively reducing resistance, are strong flocculants, distorting the behavior of individual particles in the flow. For example, pulsation velocity components in the boundary region in the turbulent flow of water and polymer solutions in a channel were obtained in [2] which differ considerably from those given in [3], where the intensity of turbulence near the wall was studied using photography of small air bubbles included in the liquid and it was established that under the conditions of a decrease in resistance there is a decrease in the intensity of the axial components of turbulent pulsations in comparison with pulsations in a Newtonian liquid, whereas no noticeable changes take place in the radial component.

In this connection it seems appropriate to develop new methods of investigation of the flow structure of turbulent streams. This is also underlined by the fact that, despite the numerous investigations, none of the existing theories ultimately satisfy the requirements of the practical use of small admixtures of polymers for the reduction of hydrodynamic resistance [4].

To study phenomena of transverse diffusion (transverse mass exchange) in the flow of polyoxyethylene solutions in a round pipe we developed a method based on the use of phenomena of nuclear magnetic resonance [5,6].

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